

KATHMANDU UNIVERSITY
End Semester Examination
March/April, 2025

Marks Scored:

Level : B.E.

Year : II

Exam Roll No. :

Time: 30 mins.

Registration No.:

Course : MCSC 201

Semester : I

F. M. : 20

Date : 08 APR 2025

SECTION "A"

[10 Q. \times 1 = 10 marks]

Fill in the blank space(s) by writing the most appropriate word(s) or symbol(s).

1. In the implication " $p \Rightarrow q$ ", the statement q is called _____.
2. The range of the characteristic function defined on subset A of universal set U is _____.
3. If $U = \{1, 2, 3, 4, 5\}$ and $A = \{1, 3, 5\}$, then the finite sequence f_A is _____.
4. A pictorial representation of a relation on a finite set is _____ of the relation.
5. A path in a graph G is called a _____ if it includes every edges exactly ones.
6. The least element of a poset, if it exists, is called a(an) _____ element.
7. A cycle of length two in permutation function is known as _____.
8. $\lfloor -2.3 \rfloor =$ _____.
9. A group $(G, *)$ is said to be abelian if _____ for each a, b in G .
10. If the function $f: \mathcal{R} \rightarrow \mathcal{R}$ be defined by $f(x) = x^2 + 1$, then $f \circ f^{-1}(71) =$ _____.

SECTION "B"
[10 Q. × 1 = 10 marks]

Fill in the blank space(s), **DO NOT TICK**, by selecting the most appropriate answers from among the given ones.

11. If 19 pigeons are assigned to 5 pigeonholes then one of the pigeonholes must contain at least _____ pigeons.
[3 ; 4 ; 5 ; 6]
12. The number of distinguishable permutations of letters in "SUNDAY" is _____.
[720 ; 760 ; 770 ; 780]
13. If $A = \begin{bmatrix} 2 & 1 \\ 3 & -2 \end{bmatrix}$ and $B = \begin{bmatrix} 1 & -1 \\ 2 & -3 \end{bmatrix}$, then $BA =$ _____
[$\begin{bmatrix} -1 & 3 \\ -5 & 8 \end{bmatrix}$; $\begin{bmatrix} -1 & -3 \\ 5 & 8 \end{bmatrix}$; $\begin{bmatrix} 1 & -3 \\ -5 & 8 \end{bmatrix}$; $\begin{bmatrix} 1 & 3 \\ -5 & -8 \end{bmatrix}$]
14. If LCM (a, b) = 60, HCF (a, b) = 5 and a = 25, find b = _____
[8 ; 9 ; 12 ; 24]
15. Let L be a lattice. Then, for each a, b in L , $a \vee b = b$ if and only if _____
[$a > b$; $a \geq b$; $a < b$; $a \leq b$]
16. The matrix $M_R = [m_{ij}]$ is an symmetric relation R has the property that if $m_{ij} = 1$, then _____
[$m_{ji} = 1$; $m_{ji} = -1$; $m_{ji} = 0$; $m_{ij} = 0$]
17. If $M_R = M_R^T$, then the relation is _____
[reflexive ; symmetric ; asymmetric ; antisymmetric]
18. The group S_3 is a group of order _____
[2 ; 3 ; 6 ; 9]
19. If $f_2(n) = 2^n - 8$, then $f_2(5) =$ _____
[8 ; 16 ; 24 ; 32]
20. If the mappings $f : \mathfrak{R} \rightarrow \mathfrak{R}$, $g : \mathfrak{R} \rightarrow \mathfrak{R}$ are defined by $f(x) = 2x$, $g(x) = x + 3$, then $(f \circ g)(1) =$ _____
[2 ; 4 ; 6 ; 8]

KATHMANDU UNIVERSITY

End Semester Examination

March/April, 2025

Level : B.E.

Year : II

Time : 2 hrs. 30 mins.

08 APR 2025

Course : MCSC 201

Semester : I

F. M. : 55

SECTION "C"

[3 Q. × 7 = 21 marks]

1. Define prime number of two positive integers. If $a \mid b$ or $a \mid c$, then prove that $a \mid bc$. Also, find the GCD of the integers $a = 120$ and $b = 500$ and then write $\text{GCD}(a, b)$ as $sa + tb$, where s and t are any integers. [1+2+4]

2. Define a relation. For any two relations R and S from A to B , prove that [1+4+2]

a. $(R \cup S)^{-1} = R^{-1} \cup S^{-1}$ and b. $\overline{(R \cap S)} = \overline{R} \cup \overline{S}$.

Also, let $A = \{1, 2, 3\}$ and consider two relations $R = \{(1, 1), (1, 2), (1, 3), (2, 2), (3, 3)\}$ and $S = \{(1, 1), (1, 2), (2, 2), (3, 2), (3, 3)\}$, then verify that

$$(S \circ R)^{-1} = R^{-1} \circ S^{-1}.$$

OR

What is meant by an equivalence relation on a set? Let R be an equivalent relation on a set A then for each a, b in A , prove that $a R b$ if and only if $R(a) = R(b)$. Also, R be the relation

on A whose matrix is $M_R = \begin{bmatrix} 1 & 1 & 1 \\ 0 & 0 & 1 \\ 0 & 1 & 1 \end{bmatrix}$. Find M_{R^2} , $M_{R^{-1}}$ and $\overline{M_R}$. [1+3+3]

3. Define a poset. If (A, \leq) and (B, \leq) posets, then show that $(A \times B, \leq)$ is poset with partial order \leq define by $(a, b) \leq (a', b')$ if $a \leq a'$ in A and $b \leq b'$ in B . Also determine the greatest and least elements, if they exists, of the poset $A = \{2, 4, 6, 8, 12, 18, 24, 36, 72\}$ with the partial order of divisibility. [1+4+2]

P.T.O.

SECTION "D"
[6Q. × 4 = 24 marks]

4. Define Characteristic function. Also, Prove that $f_{A \cup B} = f_A + f_B - f_A f_B$, symbols have their usual meaning.
5. Let $A = \{1, 2, 3, 4, 5, 6\}$ and $p = (1 \ 2 \ 4 \ 3)$ and $q = (5 \ 6)$ be a permutation of A . Compute p^{-1} , p^2 , $p \circ q$ and $q \circ p$.
6. If $A = \begin{bmatrix} 1 & 0 & 1 \\ 0 & 0 & 1 \\ 1 & 1 & 0 \end{bmatrix}$ and $B = \begin{bmatrix} 1 & 1 & 0 \\ 1 & 0 & 1 \\ 0 & 0 & 1 \end{bmatrix}$, then compute $A \vee B$, $A \wedge B$ and $A \odot B$, where the symbols have their usual meanings.
7. If f is an isomorphism from $(S, *)$ and $(T, *')$, then show that f^{-1} is an also isomorphism. Also, show that the semi groups $(\mathbf{Z}, +)$ and $(2\mathbf{Z}, +)$ are isomorphism, where \mathbf{Z} is the set of all even integers.

OR

Let $(G, *)$ be a group . Then prove the following:

- (i) Identity element of a group $(G, *)$ is unique and
(ii) Inverse of any element of a group $(G, *)$ is unique.
8. What is Mathematical Induction method? Use Mathematical Induction to prove that $2 + 2^2 + 2^3 + \dots + 2^n = 2^{n+1} - 2$, for all non-negative integer n .
9. Define Euler path and Hamiltonian path. Draw a graph which is
- Both Euler Circuit and Hamiltonian circuit
 - Euler path but not Euler circuit

SECTION "E"
[5Q. × 2 = 10 marks]

10. If $n(A) = a$ and $n(B) = b$, then prove that $n(A \times B) = a \times b$.
11. If $(G, *)$ is a group where G is the set of all non-zero real numbers and $a * b = \frac{ab}{5}$ for all a, b in G . Find the identity element of G .
12. Show that the $(p \wedge (p \Rightarrow q)) \Rightarrow q$ is a tautology.
13. If R be the relation on set A whose matrix is $M_R = \begin{bmatrix} 1 & 1 & 1 \\ 0 & 0 & 1 \\ 0 & 0 & 1 \end{bmatrix}$. Prove that R is transitive.
14. Define the maximal element of poset. What are the least and greatest elements of $P(S)$ if $S = \{a, b, c\}$.

