

KATHMANDU UNIVERSITY
End Semester Examination [C]
July, 2017

Marks scored:

Level : B. E./ B. Sc.
Year : II

Course : MCSC 201
Semester : I

Exam Roll No. :

Time: 30 mins.

F. M. : 20

Registration No.:

Date : JUL 06 2017

SECTION "A"

[10 Q. × 1 = 10 marks]

Fill in the blank space(s) by writing most appropriate word(s) or symbols(s).

1. The contrapositive of the implication ' $p \Rightarrow q$ ' is
2. The set $\{x : x \text{ is real and } x^2 = -1\}$ is
3. The symmetric closure of a relation R on a set B without closure property is
4. The range of floor function is
5. The expression $00*(0\vee 1)*1$ over a set $A = \{0, 1\}$ is expression.
6. If the real valued function g is defined by $g(x) = x^3 - 1$, then $g^{-1}(26) = \dots\dots\dots$
7. The 4-base representation of 158
8. Every subgroup of an abelian group is subgroup.
9. The quotient set of an equivalence relation R on the set of positive integers $A = \mathbb{Z}^+$ defined by $R = \{(a, b) \in A \times A : a \equiv b \pmod{3}\}$, is
10. The product of an odd and an even permutation is

SECTION "B"

[10 Q. × 1 = 10 marks]

Fill in the blank space(s), DO NOT TICK, by choosing the most appropriate answer from among the given ones.

11. If a relation S on a set B is symmetric, then $\alpha = 0$, for all i , where α is
 $[m_{ii}; \quad m_{ij}; \quad m_{ji}; \quad -m_{jj}]$
12. Two elements a and b of a poset (A, \leq) are comparable if
 $[a \leq b; \quad b \leq a; \quad a \leq b \text{ or } b \leq a; \quad a \leq b \text{ and } b \leq a]$

13. If two dices are tossed and the numbers on the top faces recorded then the probability that the sum of numbers being less than 5 is
 [1/6; 2/6; 3/6; 5/6]
14. If $A = \{1, 2, 3, 4, 6\}$, R be a relation defined on A such that $a R b$ iff a is a multiple of b . Then $n(R)$ is
 [10; 11; 12; 13]
15. If two real valued functions f and g are defined by $f(x) = x^2$ and $g(x) = x + 3$, then $(g \circ f)(-1) = \dots\dots\dots$
 [-1; 2; 4; 6]
16. The sixth term of an infinite sequence defined by the recurrence relation $d_n = d_{n-1} + 4$ with $d_1 = 3$, is
 [17; 19; 21; 23]
17. If f is the mod-12 function, then $f(1259) + f(743) = \dots\dots\dots$
 [22; 24; 26; 28]
18. The cardinality of the relation R defined on a set $A = \{1, 2, 3\}$ by $R = \{(a, b) : a + b \leq 5\}$ is
 [6; 7; 8; 9]
19. If (T, v_0) is a rooted tree on a set A , then T is
 [reflexive; symmetric; asymmetric; antisymmetric]
20. Let $f : S \rightarrow T$ be a homomorphism of the semi group $(S, *)$ onto the semi group $(T, *)'$ and R be the relation on S defined by $a R b$ if, and only if $f(a) = f(b)$, for all a, b in S , then T is isomorphic to
 [S ; R ; R/S ; S/R]

KATHMANDU UNIVERSITY
End Semester Examination [C]
July, 2017

JUL 06 2017

Level : B. E./ B. Sc.
Year : II
Time : 2 hrs. 30 mins.

Course : MCSC 201
Semester : I
F. M. : 55

SECTION "C"

[3 Q. × 7 = 21 marks]

1. Define a statement and describe logical quantifier(s) relative to predicate with examples. Also, for statements p, q, r , prove that $p \wedge (q \vee r) \equiv (p \wedge q) \vee (p \wedge r)$, where symbols have their usual meanings. [1+2+4]
2. What is meant by a relation? Define union, intersection and complement operations on relations from set A to set B . Also, for given two relations R and S from A to B , prove that (i) if $R \subseteq S$, then $\bar{S} \subseteq \bar{R}$, and (ii) $\overline{R \cap S} = \bar{R} \cup \bar{S}$. [1+3+1+2]

OR

Define a composition of two relations on sets with example. If A, B , and C are three sets, R is a relation from A to B and S a relation from B to C , then show that $(S \circ R)^{-1} = R^{-1} \circ S^{-1}$. [2+1+4]

3. Define a group and a subgroup with examples. For given sets of even integers E and integers Z , prove that $(E, +)$ is a subgroup of $(Z, +)$ where '+' is the usual addition in Z . [4+3]

SECTION "D"

[6 Q. × 4 = 24 marks]

4. Use Euclidean algorithm to find GCD(a, b) for $a = 2345$ and $b = 2130$ and then express it as $sa + tb$, for some integers s and t .
5. Let $(G, *)$ and $(G', *')$ be two groups, and let $f: G \rightarrow G'$ be a homomorphism from G to G' . Then, show that (i) If $a \in G$, then $f(a^{-1}) = (f(a))^{-1}$, and (ii) If H is a subgroup of G , then the set $f(H) = \{f(h) \mid h \in H\}$ is a subgroup of G' .

OR

Prove that a complement in a bounded distributive lattice if it exists is unique.

6. For $A = Z$, the set of integers, show that the relation $R = \{(a, b) \in A \times A : a \equiv b \pmod{5}\}$ is an equivalence and then give the quotient set.

7. Define a Boolean matrix. Compute $C \vee D$, $C \wedge D$ and $C \otimes D$, symbols have their usual meanings, for the given matrices, $C = \begin{bmatrix} 0 & 0 & 1 \\ 1 & 1 & 0 \\ 1 & 0 & 0 \end{bmatrix}$ and $D = \begin{bmatrix} 0 & 1 & 1 \\ 1 & 1 & 0 \\ 1 & 0 & 1 \end{bmatrix}$. [1+3]
8. What is meant by a matrix associated with a relation defined on a finite set? Find the transitive closure of the relation $R = \{(1, 1), (1, 4), (2, 2), (2, 3), (3, 2), (3, 3), (4, 1), (4, 4)\}$ defined on a set $A = \{1, 2, 3, 4\}$, by using Warshal's algorithm. [1+3]
9. Find an explicit formula for the sequence defined by $c_n = 3c_{n-1} - 2c_{n-2}$ with initial conditions $c_1 = 5$ and $c_2 = 3$. Also, give the first four terms of the sequence. [3+1]

SECTION "E"

[5 Q. \times 2 = 10 marks]

10. Show that if any five numbers from 1 to 8 are chosen, then two of them will add to 9.
11. Consider the set $A = \{t, u, v, w, x, y, z\}$ and the relation $R = \{(t, u), (u, w), (u, x), (u, v), (v, z), (v, y)\}$. Determine if R is a tree, and if it is, find the root.
12. Draw the Hasse diagram of the lattice $(P(A), \subseteq)$, where $P(A)$ is power set defined on $A = \{a, b, c\}$.
13. Find the inverse of $A = \begin{bmatrix} 6 & 5 \\ 4 & -2 \end{bmatrix}$ and verify your result.
14. Use mathematical induction to prove that $1 + 2^n < 3^n$, for all $n \geq 2$.