

KATHMANDU UNIVERSITY  
End Semester Examination  
August/September, 2017

Marks scored:

Level : B.Sc.

Year : II

Exam Roll No. :

Time: 30 mins.

Course : MATH 217

Semester: II

F. M. : 20

Registration No.:

Date

SEP 13 2017

SECTION "A"

[10 Q. × 1 = 10 marks]

Fill in the blank space(s) by writing the most appropriate word(s) or symbol(s).

1. The order of the PDE  $u_x = u_{yy}$  is \_\_\_\_\_.
2. A solution of a differential equation which cannot be derived from the general solution but still is a solution of the given differential equation is called a(n) = \_\_\_\_\_.
3. The Wronskian of the functions  $x^2$  and  $x|x|$  is \_\_\_\_\_.
4. The general solution  $u(x, y)$  of the PDE  $u_y = u$  is \_\_\_\_\_.
5. If  $(x_1(t), y_1(t))$  and  $(x_2(t), y_2(t))$  be any two solutions of a homogeneous systems  $x'(t) = a_1x(t) + b_1y(t)$  and  $y'(t) = a_2x(t) + b_2y(t)$ , then their Wronskian is \_\_\_\_\_.
6. The solution of the nonlinear differential equation  $p^2 - 2p + 1 = 0$ ,  $p = \frac{dy}{dx}$  is \_\_\_\_\_, where  $c$  is an integration constant.
7. The model equation for the current  $I(t)$  in a closed loop of an  $RL$ -circuit with voltage  $E(t)$  is given by \_\_\_\_\_.
8. If  $J_\gamma(x)$  and  $Y_\gamma(x)$  be respectively the Bessel polynomial of first kind and second kind, then the general solution of the Bessel equation  $x^2y'' + xy' + (x^2 - \gamma^2)y = 0$  is given by  $y(x) =$  \_\_\_\_\_ where  $A$  and  $B$  are arbitrary constants.
9. The unit step function is defined by  $u(t-a) = \begin{cases} 1, & t > a \\ 0, & t < a \end{cases}$ . The representation of the function  $f(t) = \begin{cases} 1, & 0 \leq t < 1 \\ 0, & t > 1 \end{cases}$  in terms of unit step function is given by  $f(t) =$  \_\_\_\_\_.
10. The general solution to the Euler-Cauchy differential equation  $x^2y'' + 2xy' - 12y = 0$ ,  $x \neq 0$  is  $y(x) =$  \_\_\_\_\_, where  $A$  and  $B$  are arbitrary constants.

SECTION "B"  
[10 Q. × 1 = 10 marks]

Fill in the blank space(s) by selecting the most appropriate answer from among the given ones.  
(Do not tick the answer).

11. The differential equation  $y'' + y^2 = 0$  is \_\_\_\_\_.  
[ linear and homogeneous, linear and non-homogeneous,  
nonlinear and homogeneous, nonlinear and non-homogeneous ]
12. The solution of the differential equation  $9yy' + 4x = 0$  is a family of \_\_\_\_\_.  
[circle, hyperbola, ellipse, parabola]
13. The integrating factor of the non-exact differential equation  $\frac{dy}{dx} + p(x)y = q(x)$  is \_\_\_\_\_.  
[  $\int p(x)dx$ ,  $\int q(x)dx$ ,  $e^{\int p(x)dx}$ ,  $e^{\int q(x)dx}$  ]
14. The PDE  $yu_{xx} + u_{yy} = 0$  is hyperbolic if \_\_\_\_\_.  
[  $y < 0$ ,  $y = 0$ ,  $y > 0$ ,  $|y| < 1$  ]
15. The root of the characteristic equation of the homogeneous system  $x'(t) = -2y(t)$ ,  $y'(t) = \frac{1}{2}x(t)$  is \_\_\_\_\_.  
[ -1, 0, 1, -i ]
16. In the mass spring balance model equation  $m \frac{d^2x}{dt^2} + c \frac{dx}{dt} + kx(t) = f(t)$ , the constant  $c$  is called \_\_\_\_\_.  
[spring constant, damping constant, restoring force, external force]
17. A differential equation of the form  $y = px + f(p)$ , where  $p = \frac{dy}{dx}$  is known as \_\_\_\_\_ equation.  
[Euler, Cauchy, Lagrange, Clairaut]
18. If  $L\{f(t)\} = F(s)$ , then  $L\left\{\int_0^t f(u)du\right\} =$  \_\_\_\_\_, where  $L$  is the Laplace transform operator.  
[  $sF(s)$ ,  $\frac{F(s)}{s}$ ,  $s^2F(s)$ ,  $\frac{F(s)}{s^2}$  ]
19. The Legendre's polynomial  $P_2(x) =$  \_\_\_\_\_.  
[  $\frac{1}{2}(3x^2 - 1)$ ,  $\frac{1}{2}(x^2 - 3)$ ,  $\frac{1}{2}(1 - 3x^2)$ ,  $\frac{1}{2}(3 - x^2)$  ]
20. The equation  $u_{xx} + u_{yy} = f(x, y)$  is a \_\_\_\_\_ equation.  
[heat, wave, Laplace, Poisson]

KATHMANDU UNIVERSITY  
End Semester Examination  
August/September, 2017.

SEP 13 2017

Level : B.Sc.  
Year : II  
Time : 2 hrs. 30 mins.

Course : MATH 217  
Semester: II  
F. M. : 55

SECTION "C"

[3 Q. × 7 = 21 marks]

1. Find the solution  $u(x, y)$  of the Laplace equation  $u_{xx} + u_{yy} = 0$  in the rectangular region  $R: 0 < x < a, 0 < y < b$  subjected to the boundary conditions
- $$\begin{aligned} u(0, y) = 0, \quad u(a, y) = 0 \\ u(x, 0) = 0, \quad u(x, b) = f(x) \end{aligned}$$
- [3 + 4]

OR

Find the solution  $u(x, t)$  of the 1D wave equation  $u_{tt} = u_{xx}$ ,  $0 < x < L, t > 0$  using d'Alembert's method satisfying the initial conditions  $u(x, 0) = f(x)$ ,  $u_t(x, 0) = 0$  and boundary conditions  $u(0, t) = 0$ ,  $u(L, t) = 0$  for all  $t$ .

[4 + 3]

2. Discuss the method of determinant to find the solution of the homogeneous system
- $$\begin{aligned} x'(t) &= a_{11}x(t) + a_{12}y(t) \\ y'(t) &= a_{21}x(t) + a_{22}y(t) \end{aligned}$$
- Use this method to solve the homogeneous system
- $$x'(t) = 4x(t) - 2y(t), \quad y'(t) = 5x(t) + 2y(t).$$
- [3 + 4]
3. Define Wronskian of two functions  $y_1(x)$  and  $y_2(x)$ . If functions  $y_1(x)$  and  $y_2(x)$  be any two linearly dependent solutions of the differential equation  $y'' + a(x)y' + b(x)y = 0$  then show that their Wronskian is zero. Also, find any two linearly independent solutions of  $y'' - 8y' + 16y = 0$ , and then find its general solution.
- [1 + 2 + 4]

SECTION "D"

[6 Q. × 4 = 24 marks]

4. Show that  $\frac{d}{dx} [x^\gamma J_\lambda(x)] = x^\gamma J_{\gamma-1}(x)$ , where the symbols have their usual meanings.

OR

Use Rodrigue formula to derive the expression for the Legendre's polynomial  $P_4(x)$ .

5. If a resistance of 2000 ohms and a capacitance of  $5 \times 10^{-6}$  farad are connected in series with an emf of 100 volts, what is the current at  $t = 0.1$  second if  $I(0) = 0.01$  ampere?
6. Solve  $xp^2 + (y-x)p - y = 0$  where  $p = \frac{dy}{dx}$ .
7. When the air temperature is  $70^\circ\text{F}$ , an object cools from  $170^\circ\text{F}$  to  $140^\circ\text{F}$  in 0.5 hour. What is the temperature after 1 hour?

8. Find the solution of the differential equation  $(x + y + 1) \frac{dy}{dx} = 1$ .
9. Solve  $y'' + y = \cos x$ ,  $y(0) = 3$ ,  $y'(0) = 0$ .

SECTION "E"  
[5 Q.  $\times$  2 = 10 marks]

10. Solve the PDE  $x^2 u_{xx} + 2xu_x - 2u = 0$  treating as ODE.
11. Use Power series method to find the general solution  $y(x)$  of  $y' = 2y$ .
12. Find the solution of  $x^2 y'' + 3xy' + y = 0$
13. Verify that  $y = a \cos x + b \sin x$  is the solution of  $y'' + y = 0$ , where  $a$  and  $b$  are arbitrary constants.
14. Is the differential equation  $(x^3 + 3xy^2) dx + (3x^2y + y^3) dy = 0$  exact?

Mark Scored:

KATHMANDU UNIVERSITY  
End Semester Examination  
August/September, 2017

Level : B.E.

Year : II

Course : CHEG 212

Semester : II

Exam Roll No. :

Time: 30 min

F. M. : 10

Registration No.:

Date

SEP 13 2017

SECTION "A"

[20Q × 0.5 = 10 marks]

Tick the correct answers.

- Fluid property due to which mercury doesn't wet the glass is  
a. Viscosity      b. Surface tension      c. Cohesion      d. Adhesion
- The normal stress is the same in all directions at a point in a fluid when the fluid is  
a. Non-viscous      b. Incompressible  
c. Both (a) and (b)      d. Having no motion of fluid layer
- Power loss in an orificemeter is \_\_\_\_\_ that in venturimeter.  
a. Less than      b. Same as      c. More than      d. Data insufficient
- Paper pulp is an example of \_\_\_\_\_ fluid.  
a. Newtonian      b. Pseudoplastic      c. Dilatent      d. Bingham plastic
- A particle 'A' of diameter 10  $\mu\text{m}$  settles in an oil of specific gravity 0.9 and viscosity 10 poise under Stoke's law. A particle 'B' with diameter 20  $\mu\text{m}$  settling in the same oil will have settling velocity \_\_\_\_\_  
a. Same as that of A      b.  $\frac{1}{4}$  of A  
c. 2A      d. 4A
- For flow through a packed bed with Reynolds number  $< 1.0$ , the pressure drop per unit length is proportional to superficial velocity and diameter of particle by  
a.  $V_s/D_p^2$       b.  $V_s^2/D_p$       c.  $V_s^2/D_p^3$       d.  $D_p/V_s^2$
- Dimension of surface tension is  
a.  $\text{ML}^{-1}\text{T}^{-2}$       b.  $\text{MT}^{-2}$       c.  $\text{ML}^2\text{T}^{-2}$       d.  $\text{ML}^{-1}\text{T}^{-1}$
- A Bingham fluid of viscosity  $\mu = 10 \text{ Pa}\cdot\text{s}$  and yield stress  $\tau_0 = 10 \text{ kPa}$ , is shared between two parallel plates separated by a distance of  $10^{-3} \text{ m}$ . The top plate is moving with a velocity of 1 m/s. The shear stress on the plate is  
a. 10 kPa      b. 20 kPa      c. 30 kPa      d. 40 kPa
- The ratio of  $V_{\text{avg}}$  to  $V_{\text{max}}$  in case of laminar flow of a Newtonian fluid in a circular pipe is  
a. 0.5      b. 1      c. 2      d. 0.66
- Which of the following may be termed as a variable area flow meter  
a. Venturimeter      b. Orificemeter      c. Rotameter      d. Pitot tube

11. Vena-contracta pressure tapping is at a distance \_\_\_\_\_ from the position of an orifice meter of diameter 'd' fitted in a pipe.  
 a. d                      b. 0.5 d                      c. 2 d                      d. 4 d
12. For mixing or compounding of rubber and plastics, the type of mixer used is  
 a. Ribbon blenders    b. Static mixers            c. Banbury mixer        d. Planetary mixer
13. For pipe flows, head is proportional to \_\_\_\_\_ at constant capacity.  
 (where D = pipe diameter)  
 a. 1/D                      b. 1/D<sup>2</sup>                      c. 1/D<sup>5</sup>                      d. D<sup>2</sup>
14. A centrifugal pump has power = 4 H.P; speed = 800 rpm; head = 8 m and flow = 1000 l/min. If its speed is halved, the new discharge (l/min) will be  
 a. 500                      b. 200                      c. 1000                      d. 750
15. A pressure of 10 m head of water is equivalent to \_\_\_\_\_ kN/m<sup>2</sup>.  
 a. 98                      b. 9.8                      c. 49                      d. 147
16. Percentage slip in reciprocating pump where Q<sub>1</sub> refers to actual and Q<sub>2</sub> refers to theoretical, is given by  
 a. Q<sub>1</sub>/Q<sub>2</sub>                      b. Q<sub>2</sub>/Q<sub>1</sub>                      c. (Q<sub>2</sub> - Q<sub>1</sub>)/Q<sub>1</sub>                      d. (Q<sub>2</sub> - Q<sub>1</sub>)/Q<sub>2</sub>
17. The line traced by a single fluid particle as it moves over a period of time is called \_\_\_\_\_ line.  
 a. Stream                      b. Path                      c. Steak                      d. Equipotential
18. Ratio of maximum to average velocity in case of streamline flow between parallel plates is  
 a. 1                      b. 1.5                      c. 2                      d. 2.5
19. In a drag on a sphere, value of coefficient of drag 'C<sub>d</sub>' for Reynolds Number 'NRe' 1000 - 100000 is  
 a. 4                      b. 0.5                      c. 0.2                      d. 24/NRe
20. Which of the following is used as unidirectional flow valve?  
 a. Butterfly valve    b. Gate valve            c. Check valve            d. Glove valve