

KATHMANDU UNIVERSITY
End Semester Examination [C]
January, 2018

Mark Secured:

Level : B.E./B. Sc./B. Tech
Year : I

Course : MATH 104
Semester : II

Exam Roll No. :

Time: 30 mins

F. M. : 20

Registration No. :

Date JAN: 05 2018

SECTION "A"
[10Q. \times 1 = 10 marks]

Fill in the blank space(s) by writing the most appropriate word(s) or symbol(s).

1. The equivalent Cartesian equation of $1 = \cos\theta\sin\theta$ is
2. The gradient of $f(x, y, z) = x^2 + y^2 + z^2$ at point (1, 2, 3) is
3. The double integral $\iint r dr d\theta$ over \mathbf{R} gives theof the closed and bounded region \mathbf{R} in polar form.
4. If $1 - \frac{x^2y^2}{3} < \frac{\tan^{-1}xy}{xy} < 1$ for all real values of x and y , $\lim_{(x,y) \rightarrow (0,0)} \frac{\tan^{-1}xy}{xy}$ is
5. $\left(\frac{\partial w}{\partial y}\right)_x$ is, if $w = x^2 + y^2 - z^2$, $z = x - y$.
6. The polar equation for the circle through the origin with radius 2 and center at (3, 0) is
7. $\int_0^2 \int_0^2 \int_0^2 dz dx dy = \dots\dots\dots$
8. The value of $\Gamma\left(\frac{1}{4}\right)\Gamma\left(\frac{3}{4}\right)$ is....., where $\Gamma(n)$ denotes the gamma function of n .
9. The fourier coefficient a_n of a function $f(x)$ of period 2π is defined by the formula $a_n = \dots\dots\dots$
10. The gradient field of $f(x,y,z) = xyz$ is.....

SECTION "B"
[10Q. \times 1 = 10 marks]

Fill in the blank space(s), DO NOT TICK, by selecting the most appropriate answers from among the given ones.

11. The primitive period of $\tan nx$ is.....

$\left[2\pi; \quad \pi; \quad \frac{\pi}{n}; \quad \frac{2\pi}{n} \right]$

12. The curve $r = 5 + 5\cos\theta$ is symmetric about
- [*x* - axis; *y* - axis; origin; line $y = x$]
13. $\beta(2, 3) = \dots\dots\dots$ where $\beta(m, n)$ denotes the beta function of m, n
- $\left[\frac{1}{10}; \quad \frac{1}{12}; \quad \frac{1}{14}; \quad \frac{1}{16} \right]$
14. The vector field \vec{F} is conservative if and only if $\vec{F} = \dots\dots\dots$, where f is the scalar potential function.
- $[\nabla f; \quad \nabla F; \quad \nabla \times f; \quad \nabla \cdot f]$
15. The directrix of the parabola $r = \frac{25}{10 + 10\cos\theta}$ is
- $\left[5; \quad 2; \quad \frac{5}{2}; \quad \frac{2}{5} \right]$
16. The curvature of a circle with radius r is
- $\left[r; \quad 2r; \quad \frac{r}{2}; \quad \frac{1}{r} \right]$
17. If $f(x, y, z) = xy + z$ with $x = \cos t, y = \sin t, z = t$, then $\frac{df}{dt}$ at $t = 0$ is
- $[0; \quad 1; \quad 2; \quad 3]$
18. The plane containing unit tangent vector and binormal vector is called
- [*principal plane*; *rectifying plane*; *osculating plane*; *normal plane*]
19. The polar equation $r^2 = \cos 2\theta$ is the
- [*circle*; *cardioid*; *lemniscate*; *four leaved rose*]
20. If $f(x)$ is odd function, $\int_{-a}^a f(x) = \dots\dots\dots$
- $\left[0; \quad 2 \int_0^a f(x); \quad \int_a^{-a} f(x); \quad 2 \int_{-a}^a f(x) \right]$